

Using Coloured Petri Nets for Resource Analysis of Active Objects

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Abstract. Pay-on-demand resource provisioning is an important driver for cloud computing. Virtualized resources in cloud computing open for resource awareness, such that applications may contain resource management strategies to modify their deployment and reduce resource consumption. The ABS language supports the modelling of deployment decisions and resource management for active objects. In this paper, the semantics of ABS is captured directly as a Coloured Petri Net (CPN) model capable of representing any ABS program by an appropriate initial marking. We define an abstraction relation between the CPN model and the language semantics such that markings of the CPN model become abstract ABS configurations. We use a CPN model checker as an abstract interpreter to investigate resource distribution and starvation problems for deployed active objects in ABS.

1 Introduction

Pay-on-demand resource provisioning is an important driver for cloud computing. Using resources on the cloud, a service provider does not need to cater hardware resources upfront to deploy the service but can lease resources as required by the deployed service. Resources may be dynamically added or removed depending on the traffic to a service. The enabling virtualization technology introduces a software layer representing hardware resources, which means that deployment decisions can be programmed. Virtualized resources open for resource awareness, such that applications may contain resource management strategies to modify their deployment and reduce resource consumption. In this context, it is interesting to analyze deployment scenarios for services with respect to client traffic to, e.g., establish the amount of resources required for the timely delivery of a service.

Programming models which *decouple* control flow and communication, such as Actors [1, 2] and active objects [9, 16, 26], inherently support both scalability (as argued with the Erlang programming language [5] and Scala's actors [22]) and compositional reasoning [12, 17, 18]. These features are also interesting for distributed services which should adapt to elastic cloud deployment.

In this paper, we develop a method to investigate resource distribution for deployed active objects in ABS by a translation into Coloured Petri Nets (CPNs) [25]. ABS is a formally defined active object language [26, 29] which directly supports the modelling of deployment decisions and resource management for active objects. CPNs extend the basic Petri net model [33] with data and data manipulation. We extend previous work [19] from behavioural models to deployment models such that the formal semantics of deployment models in ABS is captured directly as a hierarchical CPN. Consequently, the number of places in the CPN model is independent of the size of a program, and different programs are captured by changing the initial marking of the CPN model. This also allows the dynamic launch of virtual resources by the firing of CPN transitions. We define an abstraction relation between the CPN model and the language semantics. The model checker of CPN Tools is used as an abstract interpreter to investigate resource distribution and starvation problems for deployed active objects in ABS.

The main contributions of this paper are: (1) a *formal model* of deployed ABS programs as a hierarchical CPN that reflects the ABS semantics with markings as abstract configurations; (2) an *abstraction relation* translating resource-aware ABS programs into CPN markings and a *proof of correctness* of the abstraction relation; and (3) management support for deployment decisions in terms of *automated resource analysis* of starvation freedom and resource redistribution.

The paper is organized as follows: Section 2 introduces the ABS language, focusing on the modelling of deployment, and Section 3 briefly introduces CPNs. Section 4 presents the CPN model of the ABS semantics and Sect. 5 the abstraction relation between the CPN model and the ABS semantics, as well as the sketch of the soundness proof. The interested reader can find the full proof in a companion technical report [20]. Section 6 shows how the CPN Tools model checker can be used for the resource analysis of ABS programs. Finally, Sect. 7 draws some conclusions and discusses related work.

2 Deployment Modelling in ABS

ABS [26] is a formally defined actor-based language for the executable modelling of distributed, object-oriented systems. ABS supports *deployment modelling* by a separation of concerns between the resource costs of executions and the resource capacities of *deployment components* on which executions take place [29]; deployment components can be understood as (virtual) locations for computation. Deployment decisions can be made inside models, by allocating objects to deployment components with given resources at creation time (e.g., [4, 27]).

ABS consists of a functional layer to express computation, an imperative layer to express communication and synchronization, and a deployment layer to express deployment decisions. In this paper we elide the functional layer to focus on control flow and deployment; the relevant syntax is shown in Fig. 1. A program consists of class definitions which contain field declarations and method definitions, and a main block. We follow the syntactic conventions of Java and only explain syntax that differs from Java.

Syntactic categories. Definitions.

s in STMT	$P ::= \overline{CL} \{ \overline{T} \overline{x}; ws \}$
e in EXPR	$CL ::= \mathbf{class} C (\overline{T} \overline{x}) \{ \overline{T} \overline{x}; \overline{M} \}$
g in GUARD	$M ::= T m (\overline{T} \overline{x}) \{ \overline{T} \overline{x}; ws \}$
	$s ::= \mathbf{skip} \mid x = rhs \mid [\mathbf{DC}:e] x = \mathbf{new} C(\overline{e}) \mid \mathbf{suspend} \mid \mathbf{await} g$
	$\mid \mathbf{if} e \{ ws \} \mathbf{else} \{ ws \} \mid \mathbf{while} e \{ ws \} \mid \mathbf{return} e$
	$ws ::= s \mid [\mathbf{Cost}: e] s \mid ws; ws$
	$rhs ::= e \mid e!m(\overline{e}) \mid x.\mathbf{get}$
	$g ::= x? \mid \mathbf{duration}(e, e) \mid g \wedge g$

Fig. 1. ABS syntax. Overbar notation denotes lists.

The *imperative layer* of ABS is used for internal control flow, and for communication and synchronization between concurrent objects. Objects are instantiated from classes by the statement $[\mathbf{DC}: server] o = \mathbf{new} C(\overline{e})$, where the optional annotation $\mathbf{DC}: server$ expresses the deployment component on which the object should be created and \overline{e} are constructor arguments. A reserved field **thisDC** points to the object's deployment component, just like **this** points to the object's identifier. Concurrent objects execute processes which stem from asynchronous method calls and terminate upon method completion. Asynchronous method calls $f = o!m(\overline{e})$ are non-blocking and return a future, i.e., a placeholder for the method reply (see, e.g., [9]). The blocking expression $f.\mathbf{get}$ retrieves the return value from a future f .

Objects combine reactive and active behaviour (i.e., a run method is automatically activated upon object creation) by means of *cooperative scheduling*: Processes in an object may suspend at explicit scheduling points, allowing the scheduler to transfer control to another enabled process. Between the scheduling points, only one process is active in each object, so race conditions are avoided. Unconditional scheduling points are expressed by the statement **suspend**, conditional scheduling points by **await** g , where g may be a *synchronization condition* on a future, written $f?$ (where f points to a future) or a *duration guard*, written **duration**(b, w) where b and w are bounds on the time interval before the condition becomes true. ABS supports the modelling of dense time [8]; the local passage of time is expressed in terms of durations (as in, e.g., UPPAAL [31]).

Deployment models capture physical or virtual infrastructure in ABS using dynamically created *deployment components* [28, 29] to represent computing environments. A deployment component is a modelling abstraction which captures locations offering (restricted) resources to computations. Deployment components are created as instances of a special class DC which takes as parameter a number expressing the resource capacity of the deployment component per time interval. These components implement a method **transfer**(dc, e) which enables *vertical scaling* by shifting up to e resources to a target deployment component dc . This is in contrast to the horizontal scaling which is realized by the dynamic allocation of deployment components. ABS also supports cost annotations to model resource consumption. Thus, *weighted statements* ws are statements $[\mathbf{Cost}: e] s$ which express that e resources are required to complete execution of the statement s . In

$$\begin{array}{c}
\text{(NEW-DC)} \\
\frac{\text{fresh}(dc) \quad \llbracket e \rrbracket_{aol} = n}{o(a, \{l \mid x = \mathbf{new\ DC}(e); s\}, q)} \\
\rightarrow o(a, \{l \mid x = dc; s\}, q) \quad dc(n, 0, n)
\end{array}
\qquad
\begin{array}{c}
\text{(RUN-TO-NEW-INTERVAL)} \\
\frac{\text{blocked}(cn, t)}{0 < d \leq \text{mte}(cn, t) \quad [t] = t + d} \\
\rightarrow_t \{ \text{timeAdv}(\text{rscRefill}(cn), d) \quad cl(t + d) \}
\end{array}$$

$$\begin{array}{c}
\text{(COST1)} \\
\frac{a(\text{thisDC}) = dc \quad an = \text{Cost}: e \quad \llbracket e \rrbracket_{aol} = c \quad c \leq n - u}{o(a, \{l \mid [an'] s\}, q) \quad cn \rightarrow o(a', p', q') \quad cn'} \\
\rightarrow o(a', p', q') \quad dc(n, u + c, k) \quad cl(t) \quad cn'
\end{array}
\qquad
\begin{array}{c}
\text{(COST2)} \\
\frac{a(\text{thisDC}) = dc \quad an = \text{Cost}: e \quad \llbracket e \rrbracket_{aol} = c \quad c > n - u \quad n \neq u \quad c' = c - (n - u) \quad an' = \text{Cost}: c'}{o(a, \{l \mid [an] s\}, q) \quad dc(n, u, k) \quad cl(t) \quad cn} \\
\rightarrow o(a, \{l \mid [an'] s\}, q) \quad dc(n, n, k) \quad cn
\end{array}$$

$$\begin{array}{c}
\text{(TRANSFER)} \\
\frac{\text{fresh}(f) \quad \llbracket e \rrbracket_{aol} = dc \quad \llbracket e' \rrbracket_{aol} = dc' \quad \llbracket e'' \rrbracket_{aol} = i \quad i' = \min(i, k)}{o(a, \{l \mid x = e!\mathbf{transfer}(e', e''); s\}, q) \quad dc(n, u, k) \quad dc'(n', u', k')} \\
\rightarrow o(a, \{l \mid x = f; s\}, q) \quad dc(n, u, k - i') \quad dc'(n', u', k' + i') \quad f(i')
\end{array}$$

Fig. 2. Semantics of the deployment layer of ABS (based on [29]).

this paper we model so-called elastic computing resources, where the computation *speed* of virtual machines is determined by the amount of elastic computing resources allocated to these machines per time interval. The computation time of processes depends on the available resources of their deployment component and on how many other processes are competing for these resources.

Semantics. The semantics of ABS is given by a (transitive) transition relation \rightarrow over configurations realizing a maximal progress time model, in which time will only advance if the execution is otherwise blocked. We here focus on the transition rules formalizing the *cost and deployment aspects* of the execution of ABS programs. Configurations include *objects* $o(a, p, q)$, where o is the identifier, a the state, p the active process, and q the queue of suspended processes; *futures* $f(v)$ with identifier f and return value v ; and *deployment components* $dc(n, u, k)$ with identifier dc , n resources available in the current time interval, u resources already used in the current time interval, and k resources available in the next time interval. Technically, the deployment components book-keep the resource consumption of their allocated objects per time interval. Thus, in NEW-DC, a new deployment component with a fresh identifier dc is created, with n resources available in both the current and the next time interval. Rule RUN-TO-NEW-INTERVAL captures the advance of time. Here, the brackets enclose all objects in the configuration as well as a global clock $cl(t)$ such that time advances uniformly. The predicate $\text{blocked}(cn, t)$ expresses that no (further) reduction is possible in cn at time t , so time may advance. Let $\text{mte}(cn', t)$ denote the maximal time advance until $\text{enabled}(cn')$. The condition $[t] = t + d$ expresses that time advance has arrived at the next resource provisioning (a corresponding rule without this condition advances time without resource provisioning). Two auxiliary functions recursively change the state cn' : *timeAdv* decrements counters for **duration**-expressions and *rscRefill* provisions resources in the deployment components by changing each $dc(n, u, k)$ to $dc(k, 0, k)$.

Rule `COST1` removes the cost annotation of a statement if the associated deployment component has sufficient resources to execute the statement in the current time interval. Rule `COST2` reduces the remaining cost of executing a statement if the deployment component can provision some but not all of the required resources. Rule `TRANSFER` shifts e'' resources from a deployment component e to another deployment component e' , up to the amount of resources that e has allocated for the next time interval. This change only affects e' for the next time interval. For further details on the semantics of deployment components in ABS, we refer to [29].

3 Coloured Petri Nets

Petri nets capture true concurrency in terms of causality and synchronization [33]. A basic (low-level) Petri net constitute a directed bipartite graph comprised of places and transitions connected by arcs. An arc (p, t) is outgoing for a place p and incoming for a transition t , whereas an arc (t, p) is incoming for p and outgoing for t . Places are used to model the states of the system and may hold tokens. A marking consists of a distribution of tokens on the places of the Petri net and represent a state of the modelled system. Transitions are used for modelling the actions of the system. A transition is enabled in a marking when there is a token on each of its input places. An enabled transition may occur (fire) and the effect of occurrence is to consume a token from each input place of the transition and add a token to each of its output places. This in turn changes the current marking of the Petri net model.

Coloured Petri Nets (CPNs) is a well-established form of high-level Petri nets [25]. High-level Petri nets extend the basic Petri net formalism to enable the modelling of data and data manipulation. Each place in a CPN has an associated type determining the data values that tokens residing on the place may have, i.e., the tokens in a place represent individual values of that type. The types, representing sets of values, are called *colour sets* and individual values are seen as colours. A type can be arbitrarily complex, defined by many sorted algebra in the same way as abstract data types. A place may in general hold a multi-set of token values over the type of the place. Arcs have associated arc expressions and transitions may have an associated boolean guard expression. These expressions may contain free variables which needs to be bound to values in order to determine whether a transition is enabled, i.e., whether the required tokens are present on input places and whether the guard evaluates to true. Similarly, the multi-set of tokens removed from input places and added to output places when an enabled transition occurs are determined by evaluating the arc expression of the transition according to the values bound to the free variables.

Below we formally define CPNs [25] in their basic form without hierarchical modules. In the rest of the paper we use hierarchical CPNs. Hierarchies enrich CPNs with modularity in order to support the practical modelling of large systems. The basic definition of CPNs suffices for our purposes as any hierarchical CPN can be unfolded to a semantically equivalent non-hierarchical CPN.

Definition 1 (Coloured Petri net). A coloured Petri net (CPN) is a tuple $(P, T, A, \Sigma, V, C, G, E, I)$ where

1. P is a finite set of places P and T is a finite set of transitions T such that $P \cap T = \emptyset$;
2. A is the set of arcs, such that $A \subseteq (P \times T) \dot{\cup} (T \times P)$;
3. Σ is a finite set of non-empty types (colour sets);
4. V is a set finite set of typed variables V such that $\text{type}(v) \in \Sigma$ for all $v \in V$;
5. $C : P \rightarrow \Sigma$ is a colouring function associating a type to each place;
6. $G : T \rightarrow \text{Expr}_V$ and $E : A \rightarrow \text{Expr}_V$ are labelling functions associating expressions with free variables from V to transitions and arcs, respectively such that $\text{type}(G(t)) = \text{bool}$ for all $t \in T$ and $\text{type}(E(a)) = C(p)_{MS}$ where p is the place connected to a and $C(p)_{MS}$ denotes the multi-set type over $C(p)$.
7. $I : P \rightarrow \text{Expr}_\emptyset$ is an initialization function associating a closed expression to each place specifying the initial marking of the place such that $\text{type}(I(p)) = C(p)_{MS}$ for all $p \in P$

4 A CPN Model of ABS Semantics

In [19] the authors presented a CPN, modelling the concurrency of ABS. Active objects in [19] were represented as tokens whose colour contains their identifier and process pool. The process pool was implemented as a list, the head of which was the active process and the tail the list of the processes that were candidates to be activated by the scheduler. This list was being updated according to the calling methods of the other objects following the communication mechanism of ABS. In this paper, we focus on the deployment part of ABS. We present a new hierarchical CPN, modelling the deployment fragment of the language. Recall here, that hierarchies in CPNs introduce modularity. Each submodule can be seen as a "hidden part" of the net, named as the rectangular tag below the corresponding so-called *substitution transition* (in the figures they have double outer lines). Similarly, the double lined places keep the input/output marking of each submodule. In our CPN, we modelled the life time of program execution in a cyclic way, where the resources are refilled at the completion point of each cycle. This is illustrated in Fig. 3 where the top-layer of the model is shown. In the bottom part of this figure, we see the resource refill before the process execution in the next cycle.

We take as an input tokens that can be produced from the imperative part [19] of ABS as described above and we add information concerning the cost of each process and the deployment component they are located. This information, together with the deployment semantics of ABS can be used to verify starvation freedom of active objects and explore resource management strategies.

In the rest of the section, we present the CPN model which follows the corresponding semantic rules of ABS that add resource awareness through a running example. It is inspired from the change of the calling behaviours of cellphone clients during new year's eve midnight. Based on this example, we

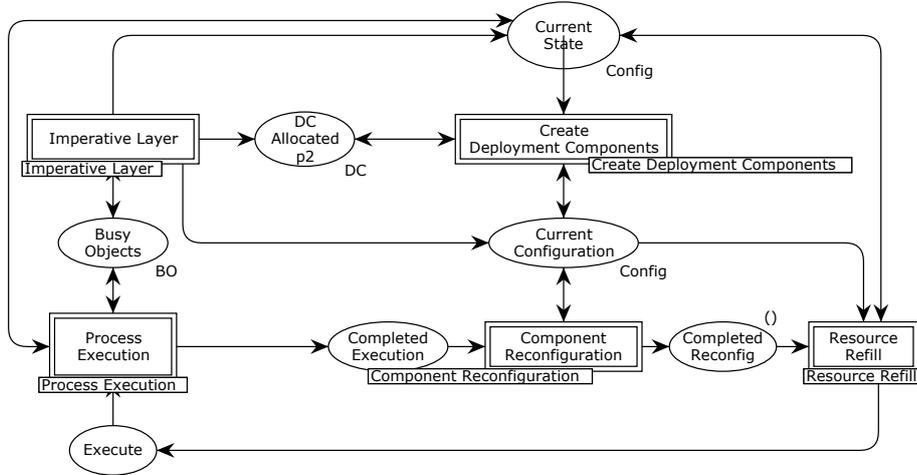


Fig. 3. Top-level module of the CPN deployment model

show in Sect. 6 how resource reallocation between deployment components can be used for load balancing purposes.

4.1 Telephone and SMS Services at Midnight on New Year's Eve

We use a running example inspired from cellphone clients behaviour in order to illustrate the relation between the CPN model and ABS programs and to show how we can use the model checker of CPN Tools for load balancing scenarios.

The average demand on phone calls and SMS messages from cellphone clients during the year is relatively low and the available resources suffice in a current distribution. There are some particular moments of the year like, for example, around the midnight of new year's eve, where this behaviour changes and a large number of SMS is requested by the clients while the call requests are negligible. Then, the initial distribution is not adequate, since there is a lack of resources for the SMS and an overplus for the calls.

In Fig. 4, we provide the ABS implementation of the above scenario [29] where telephone and SMS servers have been realised with the two corresponding classes and the operational cost annotated in square brackets at the beginning of the statements. We see that each SMS has cost 1 and each call has cost proportional to its duration. Cellphone clients can be implemented with corresponding classes allowing objects to make method calls to the SMS and telephone services.

As mentioned above, we use CPNs to model the deployment part of ABS. The markings shown in the current section are related to our running example. It is important to note that our CPN model is parametric and different ABS programs can be analysed by setting the initial marking accordingly. In our example, we modelled the SMS and the telephone servers in CPNs as two different tokens

```

1 class TelephoneServer{
2   Unit call (Int calltime) {
3     while (calltime > 0) { [Cost:1] calltime = calltime - 1; await duration (1,1); }
4   }
5 }
6 class SMSServer {
7   Unit sendSMS () { [Cost:1] skip; }
8 }
9 { // Main block
10  DC telcomp = new DC(1);
11  DC smscomp = new DC(2);
12  [DC: smscomp] SMSServer sms = new SMSServer();
13  [DC: telcomp] TelephoneServer tel = new TelephoneServer();
14  // Start client handsets...
15 }

```

Fig. 4. Implementation of Telephone and SMS Service.

representing the corresponding objects of Fig. 4 (TelephoneServer and SMSServer). Those tokens have as colour triples of the form (ob, dc, lst) , where ob is the object identifier and dc is the deployment component of the object execution. The last component (lst) models the client behaviour. In particular, it represents the process pool of the server object that keeps all the processes created from the clients calls to the corresponding service. Each process comes along with the cost of its execution, so lst is a list of triples $(proc, cost, bool)$, where $bool$ is a flag indicating whether the process has completed its execution.

Figure 5 shows the CPN module representing the imperative layer of ABS. Initially, the model has one token in place **Ready** and the transition **Imperative Layer** is enabled. Recall that the colour of the object tokens have the form (ob, dc, lst) as explained above. In Fig. 5, we have two tokens produced in place **Busy Objects**. The first one represents the object TelephoneServer with identifier 1 located in the first deployment component having in its process pool two processes: one with identifier 1 and cost 2 and one with identifier 2 and cost 4. The boolean flags set to *false* indicate that the processes have not been executed yet (it can be changed to true after firing **Process Completed**). Similarly, the second token represents the SMSServer object. Place **DC Allocated** is a counter of the deployment components created so far (for details, see [20]). Places **Current State** and **Current Configuration** have as a colour set a list of pairs (dc, cap) referring to the capacities of each deployment component. Place **Current State** keeps the current resource distribution while place **Current Configuration** records the distribution that will take place in the next cycle (resp. next time interval in ABS).

Figure 6 shows that when transition **Reconfigure** fires, the marking of the place **Current Configuration** is updated according to the function **Transfer** of its incoming arc inscription:

```

fun Transfer (fromdc,todc) cap config = List.map (fn (dc,ccap) =>

```

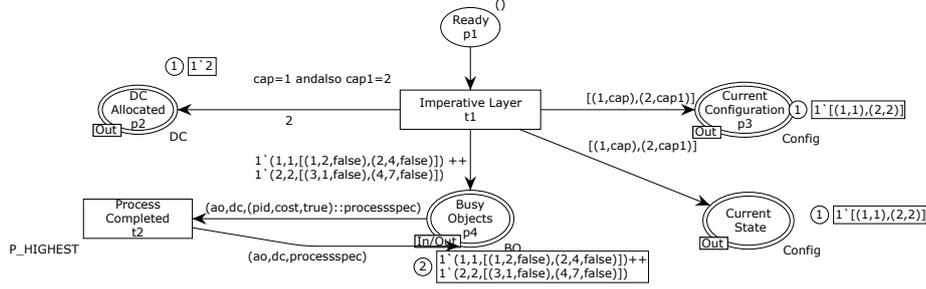


Fig. 5. CPN module of the imperative layer

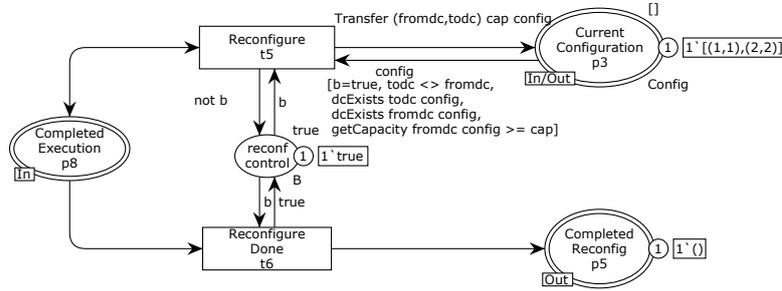


Fig. 6. CPN module for component reconfiguration

```

if (dc = fromdc) then (dc, ccap - cap) else (if (dc = todc) then (dc,
    ccap+cap) else (dc, ccap)) config
    
```

This function transfers resources from one deployment component to another. When transition **Reconfigure Done** fires, the reconfiguration has been completed. Then the resources can be refilled (details of the related implementation can be found in [20]), and the marking of the place **Current State** can be updated according to the function **Transfer** and proceed to the execution.

Figure 7 shows the module related to the process execution and the resource consumption. Places **Busy Objects** and **Current State** are fusion places (i.e they appear in more than one module and share the same marking). Recall the meaning of their markings from Fig. 5. Object 2 needs for the execution of its first process in the list (having identifier 3) 1 resource and the availability of the second deployment component according to the marking of the place **Current State** is 2 resources (having colour (2, 2)). As a result, transition **Fully Executable** (Figure 7) can fire and set its cost to zero and the boolean flag to *true* (recall that the boolean flag is related to whether the process has been fully executed or not). After this, transition **Process Completed** of Fig. 5 is enabled and the corresponding element of the list (head) is removed. Consider again Fig. 7: object 1 needs 2 resources

Before introducing the abstraction function, we note that in ABS, configurations are multi-sets containing the objects and the deployment components. Recall also that each object contains a unique object identifier, information about the deployment component to which it is located, an active process that is currently under execution, and a pool of processes that are the candidates to be executed. Below, we introduce the abstraction function α and represent all the above information at the level of tokens. Hence, we need first to define the corresponding sets and then to proceed to the definition of the abstraction function. We represent the set of ABS program configurations with \mathcal{C} , the set of the active objects of the program as Obj , the set of the deployment components as Dc , and the set of the processes as $Proc$.

We can now define the functions ob and dc mapping configurations to objects and deployment components, respectively, as $X : \mathcal{C} \rightarrow Y$ where $X \in \{ob, dc\}$ and $Y \in \{Obj, Dc\}$, with the obvious matching. Similarly, we define the functions pr and pp mapping objects to processes and sets of processes (process pools) as $F : Obj \rightarrow Z$, where $F \in \{pr, pp\}$ and $Z \in \{Proc, \mathcal{P}(Proc)\}$. We also define pd : $\mathcal{C} \rightarrow \mathcal{P}(Dc)$. Since each element among the objects, the deployment components and the processes has a unique identifier we use, by convention, positive natural numbers to translate it. This leads to the definition of the following injections: $L : W \rightarrow \mathbb{N}^*$ where $L \in \{obj_id, dc_id, proc_id\}$ and $W \in \{Obj, Dc, Proc\}$ (with the obvious matching). We also define a cost function, assigning to each process the cost of its execution: $cost : Proc \rightarrow \mathbb{N}$ as well as two capacity functions cap and $ncap$ related to the resource capacity of each deployment component (cap for the current and $ncap$ for the next time interval), defined as $cap : Proc \rightarrow \mathbb{N}$ (resp. for $ncap$). Also, we define the function $cc : \mathcal{P}(Dc) \rightarrow \mathcal{P}(Dc \times \mathbb{N})$, where $cc(S) \stackrel{def}{=} \{(dc_id(s), cap(s)) \in \mathbb{N}^* \times \mathbb{N} \mid s \in S\}$. Finally, we define the function $cpq : \mathcal{P}(Proc) \rightarrow \mathcal{P}(\mathbb{N}^* \times \mathbb{N} \times \mathbb{B})$, mapping the process pools (i.e. sets of processes) to sets of tuples, each representing the process identifier, the corresponding cost and a boolean flag (where \mathbb{B} is the set of booleans). In particular, $cpq(S) \stackrel{def}{=} \{(proc_id(s), cost(s), b) \in \mathbb{N}^* \times \mathbb{N} \times \mathbb{B} \mid s \in S \wedge b \in \mathbb{B}\}$. Similarly to the function cc , we define the function ncc where, instead of the function $cap(s)$ of cc we use the function $ncap(s)$.

So far, we have defined elementary functions to represent the interesting information taken from ABS configurations in order to form the appropriate colour sets that are used in the model. Recall from Sect. 4 that the colour set of the tokens representing the objects of an ABS program is (ob, dc, lst) where ob is the object identifier, dc is the deployment component where the object is located, and lst is the process pool augmented with information about the cost. More concretely, lst is a list of triples $(proc, cost, bool)$ indicating the identifier of each process, its corresponding cost and a boolean flag showing whether the execution of a process has been completed or not. Recall also that the colour set of the deployment components is a pair (dc, cap) where dc is the deployment component identifier and cap its resource capacity. The colour set of the place **Current State** represents the current resource distribution and place **Current Configuration** the distribution that will take place at the next time interval.

Now, let us define the abstraction function, which induces an abstract simulation relation between ABS program configurations and CPN tokens. For all configurations $c \in \mathcal{C}$:

$$\begin{aligned} \alpha(c) = \bigcap \{ & M \mid \exists p, p', p'' \in P \text{ s.t. } p \neq p' \neq p'' \text{ and for all } ob(c) \in Obj, \\ & ((obj_id \circ ob)(c), (dc_id \circ dc)(c), (cpq \circ pr \circ ob)(c)) \in M(p) \\ & \wedge (cc \circ pdc)(c) \in M(p') \\ & \wedge (ncc \circ pdc)(c) \in M(p'') \} \end{aligned} \quad (1)$$

where \bigcap is the intersection over sets of multi sets. Recall the colour sets of the places **Busy Objects**, **Starving Objects**, **Current Configuration** and **Current State**. The above function extracts information from ABS configurations and matches that information to the colour of the tokens of those places appropriately. At the second line of the equation, we have the information related to the tokens representing objects. They can be located either in **Busy Objects** or in **Starving Objects** place (hence the existential quantifier of the equation). The third and the fourth lines of the equation concern the deployment components and, in particular, the resource distributions for either the current or the next time interval. This information is also available at each ABS configuration, and hence the abstraction function retrieves it and matches it with the tokens located in places **Current State** and **Current Configuration** respectively.

Now, we can proceed to the correctness of the behaviour of our translation by establishing an abstract weak simulation relation between program configurations and CPN markings. For the full proof, see [20].

Theorem 1. *The markings of the CPN model are in abstract (weak) simulation relation with ABS program configurations.*

Proof. (sketch) We need to prove that, for any program configuration c , if $c \rightarrow_r c'$ for some ABS semantic rule r , then there exists a marking in the net M' and a sequence of enabled transitions w , such that $\alpha(c) \xrightarrow{w} M'$ and $\alpha(c') \subseteq M'$ (where, with \subseteq we denote the subset relation between sets of multi sets) \square

6 Resource Analysis and Management

We now show how state space exploration of the CPN model can be used to reason about starvation freedom of an ABS program. In presence of possible starvation, we show the state space of the CPN model can be used to synthesise a sequence of resource reconfigurations which can eliminate starvation. Finally, we show how the sequence of resource reconfiguration can be used to automatically obtain an implementation of a starvation free load balancer.

For the resource analysis, we rely on the model checker of CPN Tools applied on an Intel i7 3.4 GHz. We use the running example from the previous sections for illustration purposes, but our analysis approach generalises to instantiations of the CPN model. The state space for the running example has 776 nodes (states) and 1069 arcs (occurring events) and could be generated in less than 1 second.

For our analysis, we also rely on the strongly connected components (SCCs) of the state space. The SCCs could be generated in less than 1 second and contains 719 nodes (SCCs) and 988 arcs connecting the SCCs.

6.1 Resource Analysis

Section 4 covered the deployment layer as a CPN model. We obtained the execution cost of a program by adding cost tags to the tokens representing the active objects. More concretely, we matched each process of the process pool with the corresponding cost. Recall that the colour of an active object is represented as a triple (ob, dc, lst) , where ob is the object identifier, dc is the deployment component where the object is being executed, and lst is the process pool of the objects. The latter is represented as a list of triples $(proc, cost, bool)$ where $proc$ is the process identifier, $cost$ is the related execution cost to the current process, and $bool$ is boolean flag indicating whether the process has fully executed (value *true*) or not (value *false*). The head of lst represents the active process.

As shown in Fig. 7, the model has been constructed with place **Current State** which record the resource availability of each deployment component by hosting the corresponding tokens of colour (dc, cap) , where dc is the deployment component identifier and cap its resource capacity. In addition, the place **Starving Objects** holds tokens representing the objects whose execution has been blocked because of lack of resources at the current time interval. In the following, we explain in detail how to perform resource analysis using the markings of those places.

The first important information related to resource management is whether the current resource distribution provides sufficient resources for the full execution of the processes the objects have in their process pools. In other words, we need to check for *starvation freedom*. By model construction, place **Starving Objects** keeps track of the starving objects, if any. For the analysis, we implement the following Standard ML queries in CPN Tools for checking starvation freedom:

```

fun findStarvingObjects n =
  let
    val mSO = Mark.Process_Execution'Starving_Objects_p9 1 n
    val soid = List.map (fn (ao,_,_) => ao) mSO
  in soid end

fun anyStarving n = (findStarvingObjects n) <> nil
fun anySO ()      = PredAllNodes anyStarving

```

Function `findStarvingObjects` takes a state (marking) n as argument and extract the list of object identifiers from any tokens on place **Starving Objects**. Such object identifiers represent objects that are starving in state n . This function is then used in the predicate `anyStarving` which can be used to determine whether or not there are any starving objects in state n . The `anyStarving` predicate is then used as a higher-order argument to the built-in query function `PredAllNodes` which returns the list of all those states where the `anyStarving` predicate holds, i.e., all states where there are some object starving.

For our running example, CPN Tools returns a non-empty list containing several states which imply that starvation is possible. Since the current resource distribution may lead to starvation, an interesting question is *whether there exists a resource reallocation strategy leading to starvation freedom*. For that, we need to check for the existence of any terminal SCC containing states where there are no starving objects and then ask for a path leading to that state. This involves writing queries of similar complexity as was shown above and consists of:

- a function that checks whether a SCC is non-starving, i.e. whether it consist of only states where the marking of place **Starving Objects** is empty.
- a function searching for a non-starving SCC among the terminal SCCs ones.
- a function that returns the path from the initial marking to a state in one on the non-starving terminal SCCs.

In the last case, we are interested only in the information related to resource transfer. Recall that the module **Component Reconfiguration** (see Fig. 6) is related to the resource refill, and the **Reconfigure** transition related to the resource transfer. We therefore filtered the path returned from CPN Tools to show only the occurrences and binding elements of this transition, where the binding specifies the values bound to the variables of the transition. This is the synthesised sequence of the resource transfers we need to perform in order to avoid starvation. For our running example, this resulted in the following sequence of resource transfers:

```
[Component Reconfiguration'Reconfigure
(1, {b = true, cap = 1, config = [(1, 1), (2, 2)], fromdc = 1, todc = 2})
(1, {b = true, cap = 3, config = [(1, 0), (2, 3)], fromdc = 2, todc = 1})
(1, {b = true, cap = 2, config = [(1, 3), (2, 0)], fromdc = 1, todc = 2})]
```

The first line shows the module and the transition of which we get the binding elements. In the tuples that follow, "*b*" is a guard of the transition, "*cap*" is the amount of the resources we need to move, "*config*" is the current resource distribution, "*fromdc*" is the source deployment component and "*todc*" is the target deployment component. The resource transfer represented by the sequence hence provides a non-starvation strategy.

6.2 Resource Management: Load Balancing

Above, we saw how the state space analysis of the CPN model can be used to prove starvation freedom or, in case of possible starvation to synthesise a path from the initial resource distribution to a starvation free state of a terminal SCC. In the rest of this section, we will see how this path can be used in load balancing.

Recall that in ABS, the discrete time follows maximal progress semantics: the time advances when no further execution can happen. In that case, the resources are refilled according to the transfer command, if any; otherwise they are updated as in the previous time interval. Recall also that the colour of the deployment

components is (dc, cap) where the first element is the deployment component identifier and the second one its capacity. As an example, the pair $(1, 2)$ means that the deployment component 1 has a capacity of 2 resources.

Let us consider again our running example. Below follows a more detailed version of the path discussed in Sect. 6.1. For the sake of simplicity, we present only the name of the transition followed by the corresponding binding. The enumeration in the left corresponds to the respective ABS time point:

```

[Imperative Layer(1, {cap = 1, cap1 = 2})
t=0 Resource Refill(1, config = [(1, 1), (2, 2)], oldconfig = [(1, 1), (2, 2)])
...
Reconfigure(1, {b = true, cap = 1, config = [(1, 1), (2, 2)], fromdc = 1, todc = 2})
Reconfigure Done(1, {b = false})
t=1 Resource Refill(1, config = [(1, 0), (2, 3)], oldconfig = [(1, 0), (2, 0)])
...
Reconfigure Done(1, {b = true})
t=2 Resource Refill(1, config = [(1, 0), (2, 3)], oldconfig = [(1, 0), (2, 0)])
...
Reconfigure(1, {b = true, cap = 3, config = [(1, 0), (2, 3)], fromdc = 2, todc = 1})
Reconfigure Done(1, {b = false})
t=3 Resource Refill(1, config = [(1, 3), (2, 0)], oldconfig = [(1, 0), (2, 0)])
...
Reconfigure Done(1, {b = true})
t= 4 Resource Refill(1, config = [(1, 3), (2, 0)], oldconfig = [(1, 0), (2, 0)])
...
Reconfigure(1, {b = true, cap = 2, config = [(1, 3), (2, 0)], fromdc = 1, todc = 2})
Reconfigure Done(1, {b = false})
t=5 Resource Refill(1, config = [(1, 1), (2, 2)], oldconfig = [(1, 1), (2, 0)])

```

In the above path, the highlighted lines are resource transfers that will lead to a starvation free state, as we saw in Sect. 6.1. In our example, we consider two objects located in two deployment components. The first line shows the resource initialisation. The variables cap and $cap1$ refer, respectively, to the capacities of the first and the second deployment component. Hence we obtain the initial distribution: $(1, 1), (2, 2)$. During the first time interval, the highlighted line shows that we need to transfer 1 resource (variable cap) from the first deployment component (variable $fromdc$) to the second one (variable $todc$). Here, we notice that the variables are local to each transition, hence a possible name reuse (e.g. cap) should not create confusion. As a result of the first transfer, we obtain the distribution $(1, 0), (2, 3)$, as we can see at the corresponding resource refill (variable $config$) of the beginning of the second time interval (when $t = 1$). During the second time interval, we do not need to transfer resources, hence the refill of the beginning of the third time interval (when $t = 2$) updates the resources according to the last distribution, i.e. $(1, 0), (2, 3)$. Similarly, we obtain the distributions $(1, 3), (2, 0)$ when $t = 3$, $(1, 3), (2, 0)$ when $t = 4$ (no transfer) and $(1, 1), (2, 2)$ when $t = 5$.

The variable $oldconfig$ of the transition **Resource Refill** shows the available resources that we have before time advances. Because of the maximal progress semantics of ABS, the second component of each pair should be zero in all the

```

1 class Balancer(DC telcomp, DC smscomp) {
2   Unit run() {
3     telcomp!transfer(smscomp,1);
4     await duration(2,2);
5     smscomp!transfer(telcomp, 3);
6     await duration(2,2);
7     telcomp!transfer(smscomp,2);
8   }}
9 // Main block
10 ... // deployment components, etc. as before
11 new Balancer(telcomp,smscomp);
12 }

```

Fig. 8. Implementation of Load Balancer.

time intervals except the extremal ones: the first is the initialisation and the last one shows that we have remaining 1 resource at the first deployment component after the full execution of the processes of the first object. This is possible since the last state is starvation free.

From the above path information we can implement very easily a load balancer like the one of Fig. 8. We match object "1" with the telephone service and object "2" with the SMS service and we assume they are located at the deployment components "telcomp" and "smscomp", respectively, having the capacities as in the model, i.e. 1 and 2. In our load balancer we applied the strategy given by the path explained above, so we transfer 1 resource from the deployment component "telcomp" to the "smscomp" during the first time interval, 3 resources from the deployment component "smscomp" to the "telcomp" during the third time interval, and 2 resources from the deployment component "telcomp" to the "smscomp" during the fourth time interval. Notice here that each time we transfer resources, they take place at the next time interval according to the semantics of ABS.

7 Conclusions and Related Work

We have presented a CPN model of the deployment fragment of ABS [29], a resource aware programming language suitable for cloud applications. A key characteristic of our approach is that the compact modelling supported by CPNs allowed us to develop a CPN model capable of simulating any ABS program by only changing the initial marking. The main benefit of our approach is the ability to use model checking techniques to identify starvation of resource aware active objects, and to synthesise reconfiguration sequences that eliminates starvation and which in turn can be used to automatically obtain load-balancer implementations.

Some of the earliest applications of CPNs for analysis of distributed objects appeared in [30] focussing on spatial distribution of objects and not resource consumption. Early work [35] also considered simulation-based capacity planning of web-servers, but not in a context with dynamically configurable resources.

CPNs have also recently been used to analyze deadlock situations for active objects with futures by de Boer et al. [10,11] and by the authors [19], as found in the ABS language. More recent work [14] has considered the COSTA language [3] for deployment and management of cloud applications. Their work, however, focused on the deployment language and management operations. COSTA is able to approximate the computational cost of a program, but do not provide resource management. Recent work [23] has also explored evaluation of cloud deployment strategies for distributed NoSQL databases using CPN simulation, but without dynamic reconfiguration. In contrast to previous modelling of programming languages into Petri nets like Ada, Java, Orc ([24] [32] [15]) where the model depends on the program, we suggest a fixed sized model where the markings are program configuration abstractions, hence different programs can be analysed by one single model upon different initialisation (according to the abstraction function).

More broadly, process algebras [7], priced [13] and probabilistic [6] automata have been proposed for performance analysis of embedded systems with resource constraints. Also, other resource analysis on resource aware programs like [34] and [21], target to guarantee that the program cost does not exceed a resource threshold. Our work is not restricted only to the guarantee of resource sufficiency, but also in case of possible starvation, proposes strategies for vertical scaling that can be retrieved by the counter examples of CPN Tools.

Our present work extends [19] by taking as input the communication status of resource aware active objects and performing resource analysis. We demonstrated how to statically construct a load balancer. A direction for future work will be to extend the model to support dynamic load balancing and investigate optimal vertical scaling using the CPN model checker. Another direction will be to perform a comprehensive experimental evaluation on a larger set of ABS programs.

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